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# The Crystal and Molecular Structure of Tetrakis(tropolonato)zirconium(IV)-Chloroform: $\mathrm{Zr}\left(\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{O}_{2}\right)_{4} .\left(\mathrm{CHCl}_{3}\right)_{2.25}$ 

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#### Abstract

The title compound crystallizes in the triclinic space group $P \overline{1}$, with cell constants $a=11.714(3), b=$ 15.163 (4), $c=10.317$ (3) $\AA, \alpha=91.74$ (2), $\beta=73.91$ (3), $\gamma=100.94$ (2) ${ }^{\circ}$, and $Z=2.4527$ reflections were measured by counter methods using monochromatized Mo $K a$ radiation $[\lambda(\alpha)=0.70926 \AA]$. Fullmatrix least-squares refinement of the 2774 reflections classed as observed (i.e. $\geq 2 \cdot 3 \sigma$ ) gave a final $R$ factor of $7.5 \%$. The geometry about the Zr atom is very nearly dodecahedral, with an average $\mathrm{Zr}-\mathrm{O}$ bond distance of $2.177 \AA$, and an average $\mathrm{O} \cdots \mathrm{O}$ intraligand donor-atom separation of $2.493 \AA$. The two shortest $\mathrm{O} \cdots \mathrm{O}$ interligand distances in the ' $\mathrm{ZrO}_{8}$ ' polyhedron occur between adjacent ligands which are approximately coplanar, providing a further example of what appears to be a trend in high-coordinate chelate complexes. One tropolone ligand is disordered between two positions as a result of close contact with a partially occupied chloroform molecule. However, this disorder does not affect the essential geometry of the ' $\mathrm{ZrO}_{8}$ ' polyhedron.


## Introduction

The tropolonato ligand (hereon abbreviated to $T$ ), has been shown to form high-coordinate complexes with a wide variety of metals (Muetterties \& Wright, 1967). Previous structural studies have shown it to be a compact, planar ligand with a fairly constant inter-donor-atom separation (Guggenberger \& Muetterties, 1972; Davis \& Einstein, 1974, 1975). This paper reports the crystal and molecular structure of an eightcoordinate complex of this ligand with $\mathrm{Zr}^{1 \mathrm{v}}$, which may be compared to other similarly coordinated metal complexes, and its geometry is discussed in relation to the existing theory of high coordination.

## Experimental

$\mathrm{Zr}_{4}\left(\mathrm{CHCl}_{3}\right)_{2.25}$ was prepared according to the method described by Muetterties \& Wright (1967). Zirconium

[^0]tetrachloride $(0.25 \mathrm{~g}, 0.001 \mathrm{~mol})$ was dissolved in chloroform ( 20 ml ) and added with stirring to a solution of tropolone $(0.6 \mathrm{~g}, 0.0045 \mathrm{~mol})$ in chloroform $(10 \mathrm{ml})$. A further 10 ml of chloroform was added to this mixture, which was then refluxed for $\frac{1}{4} \mathrm{~h}$. Slow evaporation of the resulting brown solution gave brown/orange crystals which became yellow and amorphous when stored in the absence of chloroform. Rapid loss of chloroform of solvation and the accompanying loss of crystalline character made accurate thermogravimetric analysis impossible, and the mounting of a single crystal somewhat difficult. Finally, a single crystal of approximate dimensions $0.9 \times 0.13 \times$ 0.06 mm was sealed under an atmosphere of chloroform in a Lindemann-glass tube, and mounted along the needle axis. Cu radiation $(\lambda=1.5418 \AA)$ was used in a preliminary photographic investigation which established triclinic Laue symmetry, with the $a$ axis approximately coincident with the needle axis of the crystal. Accurate cell dimensions were determined from the counter measurement of 12 of the strongest reflections having $2 \theta>20^{\circ}$ using a Picker FACS-1
computer-controlled four-circle diffractometer (Mo $K \alpha$ radiation, $\lambda=0.70926 \AA$ ), with a take-off angle of $1.0^{\circ}$.

## Crystal data

$\mathrm{Zr}\left(\mathrm{C}_{7} \mathrm{H}_{5} \mathrm{O}_{2}\right)_{4} .\left(\mathrm{CHCl}_{3}\right)_{2.25}, \mathrm{FW} 844 \cdot 3$, crystallizes in the triclinic space group $P 1$, with $a=11.714(3), b=$ 15.163 (4), $c=10.317$ (3) $\AA, \quad \alpha=91.74$ (2), $\beta=$ 73.91 (3), $\gamma=100.94$ (2) $^{\circ}, V=1683.3 \AA^{3}, d_{m}=1.60$ (by flotation), $Z=2, d_{x}=1.67 \mathrm{~g} \mathrm{~cm}^{-3}, \mu(\mathrm{Mo} K \alpha)=$ $9.23 \mathrm{~cm}^{-1}, t=22( \pm 1)^{\circ} \mathrm{C}$.

Reflections for the unique set of data were collected in two shells using a scintillation detector with pulseheight analysis, with a symmetric $\theta-2 \theta$ scan at a speed of $2^{\circ} \mathrm{min}^{-1}$. For data where $\sin \theta<0.2164$, a scan
base width of $1.5^{\circ}$ was used, with background counts of 10 s made at both scan limits; for data where 0.2164 $<\sin \theta<0.3826$, a scan base of $0.9^{\circ}$ was used with background counts of 4 s made at both scan limits. After each seventy reflections, two standard reflections were measured; their variation was $\pm 5 \%$ over the entire data collection. The measured intensities were corrected for Lorentz and polarization effects; absorption was neglected since it was estimated to produce an extreme error of $\pm 6 \%$ in $I .4527$ reflections were measured, of which 2774 were classed as observed \{i.e. greater than $2 \cdot 3 \sigma_{I}$, where $\sigma_{I}=\left[\mathrm{TC}+\left(t_{s} / t_{b}\right)^{2}\left(B_{1}+B_{2}\right)+(k I)^{2}\right]^{1 / 2}$ and where TC is the total count, $B_{1}$ and $B_{2}$ are background counts at either end of the scan range, $t_{s}$ is the scan time, $t_{b}$ is the total background count time, $k$ is a constant set to 0.03 , and $I$ is the net count $\}$.

Table 1. Fractional atomic coordinates $\left(\times 10^{4}\right.$, for $\left.\mathrm{Zr} \times 10^{5}\right)$ in crystalline $\mathrm{Zr} T_{4} .\left(\mathrm{CHCl}_{3}\right)_{2 \cdot 25}$
Least-squares estimated errors in this and other tables are given in parentheses.

|  | $x$ | $y$ | $z$ |  | $x$ | $y$ | $z$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Zr | -22056 (8) | 18206 (7) | 7586 (11) | C(33') | 514 (22) | 5262 (15) | 1103 (24) |
| $\mathrm{Cl}(1)$ | 4221 (3) | 3422 (2) | 3829 (4) | $\mathrm{C}\left(34^{\prime}\right)$ | 1662 (21) | 5118 (16) | 711 (24) |
| $\mathrm{Cl}(2)$ | 6211 (3) | 4830 (3) | 3399 (4) | $\mathrm{C}\left(35^{\prime}\right)$ | 2058 (18) | 4360 (15) | 245 (23) |
| $\mathrm{Cl}(3)$ | 4788 (23) | 4305 (18) | 1509 (26) | C(36) | 1438 (19) | 3496 (15) | 157 (24) |
| $\mathrm{Cl}\left(3^{\prime}\right)$ | 5362 (24) | 4475 (15) | 1270 (21) | C(37) | 168 (21) | 3210 (16) | 483 (26) |
| $\mathrm{Cl}(4)$ | 709 (4) | 1362 (3) | -4078 (4) | C(41) | -3535 (16) | 2620 (7) | -1972 (15) |
| $\mathrm{Cl}(5)$ | 2106 (3) | 1451 (3) | -2197 (4) | C(42) | -4517 (11) | 2888 (6) | -1248(15) |
| $\mathrm{Cl}(6)$ | 1610 (4) | 3063 (3) | -3096 (5) | C(43) | -4589 (19) | 3193 (12) | -2455 (24) |
| $\mathrm{Cl}(7)$ | -20 (17) | 3356 (12) | 3778 (16) | C(44) | -3803 (27) | 3334 (16) | -3684 (28) |
| $\mathrm{Cl}(8)$ | -505 (17) | 5020 (15) | 4726 (26) | C(45) | -2632 (23) | 3135 (12) | -4043 (18) |
| Cl(9) | 1675 (25) | 4625 (20) | 4539 (40) | C(46) | -2043 (12) | 2790 (9) | -3245 (20) |
| $\mathrm{O}(1)$ | -1137(5) | 830 (4) | -236 (6) | C(47) | -2396 (12) | 2532 (8) | -1894 (16) |
| $\mathrm{O}(2)$ | -3376 (5) | 611 (4) | 364 (6) | C(1) | 5504 (10) | 3982 (8) | 2619 (12) |
| $\mathrm{O}(3)$ | -1796 (6) | 1258 (4) | 2436 (7) | C(2) | 1096 (10) | 1936 (8) | -2728(11) |
| $\mathrm{O}(4)$ | -3711 (6) | 1735 (5) | 2570 (9) | C(3) | 270 | 4246 | 4744 |
| O(5) | -2027(13) | 3089 (10) | 1859 (16) | H(12) | -65 | -3308 | -143 |
| $\mathrm{O}\left(5^{\prime}\right)$ | -1846 (13) | 3279 (10) | 1160 (16) | H(13) | -563 | -1564 | -2480 |
| O(6) | -1272 (5) | 2398 (5) | 382 (7) | H(14) | -2367 | -2213 | -2696 |
| O(7) | -3634 (6) | 2384 (5) | 1248 (9) | H(15) | -4145 | -1833 | -1716 |
| $\mathrm{O}(8)$ | -1670 (6) | 2245 (5) | -1346 (8) | H(16) | -4556 | -726 | -415 |
| $\mathrm{C}(11)$ | -1625 (8) | 87 (7) | -708 (10) | H(22) | -1481 | 588 | 4416 |
| C(12) | -1905 (7) | -492 (7) | -1395 (10) | H(23) | -2519 | 190 | 6468 |
| C(13) | -1213 (8) | -1266 (7) | -2036 (11) | H(24) | -4364 | 409 | 7537 |
| C(14) | -2345 (8) | -1693 (7) | -2140 (11) | H(25) | -5617 | 979 | 6741 |
| C(15) | -3458 (7) | -1446 (7) | -1541 (11) | H(26) | -5386 | 1489 | 4727 |
| C(16) | -3708 (7) | -739 (7) | -756 (10) | H(32) | -1580 | 4574 | 2966 |
| $\mathrm{C}(17)$ | -2944 (8) | -37(7) | -362 (10) | H(33) | 105 | 5534 | 3023 |
| C(21) | -2539 (9) | 1108 (7) | 3601 (13) | H(34) | 2009 | 5299 | 2363 |
| C(22) | -2281 (9) | 720 (8) | 4652 (14) | H(35) | 2730 | 4288 | 1019 |
| C(23) | -2928 (11) | 479 (8) | 5960 (13) | H(36) | 1788 | 3064 | 426 |
| C(24) | -4090 (12) | 602 (8) | 6603 (11) | H(32') | -1275 | 4889 | 1504 |
| C(25) | -4854 (10) | 960 (9) | 6106 (15) | H(33') | 435 | 5866 | 1377 |
| C(26) | -4698 (9) | 1293 (8) | 4851 (13) | H(34') | 2284 | 5623 | 764 |
| C(27) | -3687 (9) | 1396 (7) | 3689 (13) | H(35') | 2929 | 4435 | -119 |
| C(31) | -956 (18) | 3576 (14) | 1856 (22) | H(36) | 1923 | 3045 | -169 |
| C(32) | -835 (20) | 4388 (16) | 2501 (23) | H(42) | -5232 | 2857 | -515 |
| C(33) | 210 (26) | 4973 (18) | 2565 (29) | H(43) | -5356 | 3340 | -2426 |
| C(34) | 1407 (27) | 4841 (20) | 2114 (30) | H(44) | -4044 | 3592 | -4391 |
| C(35) | 1854 (21) | 4199 (17) | 1338 (27) | H(45) | -2179 | 3256 | -4976 |
| C(36) | 1276 (22) | 3457 (16) | 930 (27) | H(46) | -1240 | 2711 | -3725 |
| C(37) | -11(23) | 3131 (18) | 1112 (27) | H(1) | 6044 | 3574 | 2254 |
| $\mathrm{C}\left(31^{\prime}\right)$ | -736 (19) | 3737 (14) | 914 (23) | H(2) | 338 | 1896 | -1954 |
| $\mathrm{C}\left(32^{\prime}\right)$ | -547 (19) | 4641 (15) | 1197 (22) | H(3) | -24 | 3991 | 5627 |

## 2112 THE STRUCTURE OF TETRAKIS(TROPOLONATO)ZIRCONIUM(IV)-CHLOROFORM

## Structure determination and refinement

A three-dimensional Patterson synthesis based on all the data gave the position of the Zr atom; refinement of these atomic parameters and two scale factors (for the inner and outer shells of data) gave $R=0.439$, where $R=\sum\left(\left|F_{o}\right|-\left|F_{c}\right|\right) / \sum\left|F_{o}\right|$. A Fourier synthesis gave the positions of the eight O and the three Cl atoms of one molecule of chloroform. Several cycles of refinement and subsequent electron density difference maps gave the positions of a further molecule of chloroform and all tropolonato C atoms. With all these atoms assigned anisotropic thermal parameters, full-matrix leastsquares refinement gave an $R$ factor of $0 \cdot 101$, though it was clear that one tropolonato ligand (ligand 3) was irregular. The seven C atoms and one O at this ligand had very large components of thermal motion in a direction approximately perpendicular to the general plane of the ring, suggesting that the ring was disordered between two positions. Further, there were some large peaks still unaccounted for in the electron density difference map which were close to this disordered ring. The disorder in ligand 3 was accommodated by arranging the seven $C$ atoms and one $O$ atom $[O(5)]$ in two positions, each with half occupancy. Upon refinement of alternate occupancy factors and isotropic thermal-motion parameters, this model behaved well, with refined occupancy factors remaining at $0 \cdot 5$. The peaks thus far unaccounted for in the difference map suggested another molecule of chloroform. However, since this molecule was extremely close to a centre of symmetry, and since in either position it had close contact with one position of ligand 3 , it was assigned an occupancy of $0 \cdot 25$. A list of the short contacts which led to our model is given in Table 4 and the resulting packing within the unit cell can be seen in Fig. 4. Two further ramifications of the
presence of the partially occupied, disordered chloroform should be mentioned. When the molecule is present, ligand 3 is bent away to relieve short contacts that occur. The alternative position adopted by this ligand creates several short contacts with a further chloroform molecule of crystallization [notably atom $\mathrm{Cl}(3)$ ], with subsequent disorder imparted to this

Table 2. Bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ within the ' $\mathrm{ZrO}_{8}$ ' polyhedron of crystalline $\mathrm{Zr} T_{4} .\left(\mathrm{CHCl}_{3}\right)_{2 \cdot 25}$

| $\mathrm{Zr}-\mathrm{O}(1)$ | 2.188(6) | $\mathrm{O}(1) \mathrm{ZrO}(2)$ | 69.4 (2) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Zr}-\mathrm{O}(2)$ | 2.172 (6) | $\mathrm{O}(3) \mathrm{ZrO}(4)$ | 69.0 (3) |
| $\mathrm{Zr}-\mathrm{O}(3)$ | $2 \cdot 161$ (7) | $\mathrm{O}(5) \mathrm{ZrO}(6)$ | 71.5 (5) |
| $\mathrm{Zr}-\mathrm{O}(4)$ | 2.172 (8) | $\mathrm{O}\left(5^{\prime}\right) \mathrm{ZrO}$ (6) | $66 \cdot 6$ (5) |
| $\mathrm{Zr}-\mathrm{O}(5)$ | $2 \cdot 197$ (6) | $\mathrm{O}(7) \mathrm{ZrO}(8)$ | 68.8 (3) |
| $\mathrm{Zr}-\mathrm{O}\left(5^{\prime}\right)$ | $2 \cdot 220$ (14) | $\mathrm{O}(1) \mathrm{ZrO}(3)$ | 78.2 (2) |
| $\mathrm{Zr}-\mathrm{O}(6)$ | 2.208 (14) | $\mathrm{O}(1) \mathrm{ZrO}(6)$ | 70.7 (2) |
| $\mathrm{Zr}-\mathrm{O}(7)$ | 2.206 (7) | $\mathrm{O}(1) \mathrm{ZrO}$ (8) | 77.1 (3) |
| $\mathrm{Zr}-\mathrm{O}(8)$ | $2 \cdot 168$ (8) | $\mathrm{O}(2) \mathrm{ZrO}(3)$ | 95.9 (2) |
| $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.480 (7) | $\mathrm{O}(2) \mathrm{ZrO}(4)$ | 79.8 (2) |
| $\mathrm{O}(3)-\mathrm{O}(4)$ | 2.457 (9) | $\mathrm{O}(2) \mathrm{ZrO}(7)$ | 78.2 (2) |
| $\mathrm{O}(5)-\mathrm{O}(6)$ | 2.574 (15) | $\mathrm{O}(2) \mathrm{ZrO}(8)$ | 91.6 (3) |
| $\mathrm{O}\left(5^{\prime}\right)-\mathrm{O}(6)$ | 2.425 (15) | $\mathrm{O}(3) \mathrm{ZrO}(5)$ | 84.4 (5) |
| $\mathrm{O}(7)-\mathrm{O}(8)$ | 2.471 (10) | $\mathrm{O}(3) \mathrm{ZrO}\left(5^{\prime}\right)$ | 101.4 (6) |
| $\mathrm{O}(1)-\mathrm{O}(3)$ | 2.743 (9) | $\mathrm{O}(3) \mathrm{ZrO}(6)$ | 78.6 (3) |
| $\mathrm{O}(1)-\mathrm{O}(6)$ | 2.538 (9) | $\mathrm{O}(4) \mathrm{ZrO}(5)$ | 70.5 (5) |
| $\mathrm{O}(1)-\mathrm{O}(8)$ | 2.713 (10) | $\mathrm{O}(4) \mathrm{ZrO}\left(5^{\prime}\right)$ | 85.4 (5) |
| $\mathrm{O}(2)-\mathrm{O}(3)$ | 3.218 (8) | $\mathrm{O}(4) \mathrm{ZrO}(7)$ | $72 \cdot 5$ (3) |
| $\mathrm{O}(2)-\mathrm{O}(4)$ | 2.786 (9) | $\mathrm{O}(5) \mathrm{ZrO}(7)$ | 81.5 (5) |
| $\mathrm{O}(2)-\mathrm{O}(7)$ | 2.772 (9) | $\mathrm{O}\left(5^{\prime}\right) \mathrm{ZrO}$ (7) | 73.7 (5) |
| $\mathrm{O}(2)-\mathrm{O}(8)$ | 3.111 (9) | $\mathrm{O}(5) \mathrm{ZrO}(8)$ | 104.2 (5) |
| $\mathrm{O}(3)-\mathrm{O}(5)$ | $2 \cdot 936$ (16) | $\mathrm{O}\left(5^{\prime}\right) \mathrm{ZrO}$ (8) | 84.9 (5) |
| $\mathrm{O}(3)-\mathrm{O}\left(5^{\prime}\right)$ | $3 \cdot 390$ (16) | $\mathrm{O}(6) \mathrm{ZrO}$ (8) | 76.9 (3) |
| $\mathrm{O}(3)-\mathrm{O}(6)$ | 2.759 (10) | $\mathrm{O}(5) \mathrm{ZrO}\left(5^{\prime}\right)$ | 19.3 (5) |
| $\mathrm{O}(4)-\mathrm{O}(5)$ | 2.529 (17) |  |  |
| $\mathrm{O}(4)-\mathrm{O}\left(5^{\prime}\right)$ | 2.979 (18) |  |  |
| $\mathrm{O}(4) \cdots \mathrm{O}(7)$ | 2.589 (12) | $\mathrm{O}\left(5^{\prime}\right) \cdots \mathrm{O}(8)$ | 2.961 (16) |
| $\mathrm{O}(5) \cdots \mathrm{O}$ (7) | 2.882 (17) | $\mathrm{O}(6) \cdots \mathrm{O}$ (8) | 2.713 (10) |
| $\mathrm{O}\left(5^{\prime}\right) \cdots \mathrm{O}(7)$ | $2 \cdot 655$ (16) | $\mathrm{O}(5) \cdots \mathrm{O}\left(5^{\prime}\right)$ | 0.743 (18) |

Table 3. Parameters used to describe the ' $\mathrm{ZrO}_{8}$ ' polyhedron
(a) Values of $\delta$ and $\varphi$ (as defined by Porai-Koshits \& Aslanov, 1972) for regular polyhedra of the dodecahedra class, and for tetrakis(tropolanato) complexes of $\mathrm{Sc}^{\mathrm{III}}, \mathrm{Nb}^{\vee}$ and $\mathrm{Zr}^{\mathbf{I V}}$

|  | $\delta\left({ }^{\circ}\right)$ |  |  | $\varphi\left({ }^{\circ}\right)$ |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Dodecahedron | 29.5 | 29.5 | 29.5 | 29.5 | 0 | 0 |
| Bicapped trigonal prism | 0 | 21.7 | 48.2 | 48.2 | 16.1 | 16.1 |
| Square antiprism | 0 | 0 | 52.5 | 52.5 | 24.5 | 24.5 |
| $\mathrm{Sc} T_{4}^{-}$ | 13.4 | 29.0 | 42.3 | 43.0 | 10.8 | 10.8 |
| $\mathrm{Zr} T_{4}$ | 22.9 | 31.8 | 32.4 | 40.1 | 6.6 | 1.9 |
| $\mathrm{Nb} T_{4}^{+}$ | 19.4 | 21.0 | 42.9 | 45.1 | 11.5 | 13.9 |

(b) Angular parameters $\left({ }^{\circ}\right)$ which define the geometry of $\mathrm{Zr} T_{4}, \mathrm{Sc}_{4}^{-}$and $\mathrm{Nb} T_{4}^{+}$compared with those generated by calculation

$$
\begin{aligned}
& D_{2 d} \text { dodecahedron }(b=1.15) \\
& D_{2} \text { square antiprism }(b=1.15) \\
& \mathrm{ScT}_{4}^{-}(b=1.13) \\
& \mathrm{Zr} T_{4}(b=1.145) \\
& \mathrm{Nb} T_{4}(b=1.16)
\end{aligned}
$$

| $\varphi_{A}$ | $\varphi_{B}$ | $\theta_{A}$ | $\theta_{B}$ | $M-A / M-B$ |
| :---: | :---: | :---: | :---: | :---: |
| 39.2 | 112.3 | 45.0 | 40.6 | 1.0 |
| 37.5 | 107.1 | 33.4 | 52.5 | 1.0 |
| 36.3 | 105.5 | 37.8 | 48.3 | 1.01 |
| 35.8 | 105.6 | 44.3 | 47.9 | 1.01 |
| 35.7 | 106.3 | 37.8 | 49.7 | 1.01 |

molecule (see Table 4). The disorder is manifested in the large Cl atom thermal-motion parameters; in particular, the extreme motion exhibited by $\mathrm{Cl}(3)$ in one direction ( $z$ ) implied two alternative positions, a model which was adopted (each position being assigned an occupancy factor of 0.5 ), and which behaved well during further refinement. Some minor disorder is also imparted to ligand 4 , which is apparent from the rather high thermal parameters for the C atoms of this ring. All H atom positions were calculated. Full-matrix leastsquares refinement of all non-hydrogen atomic parameters, with all atoms assigned anisotropic thermal-motion parameters except the C atoms of ligand 3, atom $\mathrm{O}(5)$, and chloroform C atoms, gave a final $R$ factor of 0.075 .

Constant unit weights were used in the early stages of refinement; in the final stages, weights $\left\{=1 /\left[\sigma^{2}(F)\right]\right.$ where $\left.\sigma(F)=\sigma_{I} /(\operatorname{Lp})\left(2 F_{o}\right)\right\}$ were used. Atomic scattering factors used were taken from Cromer \& Waber (1974). Crystallographic computer programs used in this determination have been cited elsewhere (Einstein \& Jones, 1972). Atomic positional coordi-

Table 4. Shortest intermolecular contacts ( $\AA$ ) in crystalline $\mathrm{Zr}_{4}\left(\mathrm{CHCl}_{3}\right)_{2 \cdot 25}$ which determine the model used to describe the structure (see text and Fig. 4)
$\mathrm{Cl}\left(8^{*}\right)$ is the centrosymmetrically related alternative position of $\mathrm{Cl}(8)$ in the disordered $\mathrm{CHCl}_{3}$ molecule of solvation.

| $\mathrm{H}(32)-\mathrm{Cl}(8)$ | 2.49 | $\mathrm{C}(33)-\mathrm{Cl}(9)$ | 2.89 |
| :--- | :--- | :--- | :--- |
| $\mathrm{H}(33)-\mathrm{C}(3)$ | 2.34 | $\mathrm{C}(33)-\mathrm{C}(3)$ | 2.92 |
| $\mathrm{H}(33)-\mathrm{Cl}(8)$ | 1.79 | $\mathrm{C}(34)-\mathrm{C}(3)$ | 2.58 |
| $\mathrm{H}(33)-\mathrm{Cl}(9)$ | 2.72 | $\mathrm{C}(35)-\mathrm{Cl}(7)$ | 2.97 |
| $\mathrm{H}(33)-\mathrm{H}(3)$ | 1.52 | $\mathrm{C}(36)-\mathrm{Cl}(7)$ | 2.90 |
| $\mathrm{H}(34)-\mathrm{Cl}(9)$ | 2.33 | $\mathrm{C}(37)-\mathrm{Cl}(7)$ | 2.79 |
| $\mathrm{C}(31)-\mathrm{Cl}(7)$ | 2.59 | $\mathrm{H}\left(35^{\prime}\right)-\mathrm{Cl}\left(3^{\prime}\right)$ | 2.40 |
| $\mathrm{C}(32)-\mathrm{Cl}(7)$ | 2.56 | $\mathrm{H}(46)-\mathrm{H}(3)$ | 2.18 |
| $\mathrm{C}(32)-\mathrm{Cl}(8)$ | 2.56 | $\mathrm{H}(45)-\mathrm{Cl}(7)$ | 2.50 |
| $\mathrm{C}(33)-\mathrm{Cl}(7)$ | 2.62 | $\mathrm{H}(46)-\mathrm{Cl}(7)$ | 2.70 |
| $\mathrm{C}(33)-\mathrm{Cl}(8)$ | 2.03 | $\mathrm{C}(46)-\mathrm{H}(3)$ | 2.70 |
| $\mathrm{C}(33)-\mathrm{Cl}\left(8^{*}\right)$ | 2.83 |  |  |



Fig. 1. A perspective view of the $\mathrm{Zr} T_{4}$ molecule, illustrating the thermal-motion ellipsoids ( $50 \%$ ) and labelling. The alternative position of ligand 3 (as explained in the text) is shown in outline.
nates are listed in Table 1.* Table 2 shows the bond lengths and angles of the ' $\mathrm{ZrO}_{8}^{\prime}$ ' polyhedron, and Table 3 lists the parameters used to describe this polyhedron. Table 4 gives selected intermolecular contacts relevant to the model used to describe the disorder present in the structure. Fig. 1 is a perspective view of the $\mathrm{Zr}_{4}$ moiety, Fig. 2 outlines the $\mathrm{ZrO}_{8}$ coordination polyhedron, Fig. 3 shows the generalized eight coordination relevant to the discussion, and Fig. 4 illustrates the packing within the unit cell.

## Discussion

## The ' $\mathrm{ZrO}_{8}$ ' polyhedron

The procedure described by Porai-Koshits \& Aslanov (1972) is used to describe the coordination

* Lists of structure factors and anisotropic thermal parameters have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 33336 ( 33 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.


Fig. 2. A perspective view of the distorted dodecahedron formed by the eight O donor atoms in $\mathrm{Zr}_{4}$. The direction of the approximate 4 axis is shown by the broken line.


Fig. 3. A diagram of the generalized eight coordination used in the discussion, showing labelling of the angular parameters. [The labelling of the angular parameters used in this discussion differs from those used previously by us. The change has been made to make the labelling consistent with similar work on six coordination (Kepert, 1978).]


Fig. 4. A view (along $\mathbf{c}$ ) of the unit cell of $\mathrm{Zr}_{4}$. $\left(\mathrm{CHCl}_{3}\right)_{2.25}$, illustrating the packing and the disorder in ligand 3 (as described in the text).
polyhedron formed by the eight O atoms. [In this discussion, the position adopted by ligand 3 when the nearby chloroform molecule is present is ignored; the atomic coordinates of atom $O(5)$ are used, rather than $\mathrm{O}(5)^{\prime}$.] The polyhedron is described by the four values of $\sigma$, the angle between pairs of faces which intersect along those edges which connect vertices at which five edges are joined. These vertices are seen in Fig. 2 as $O(5), O(2), O(8)$ and $O(3)$. Also, the angles $\varphi$ which indicate the degree of nonplanarity of the intersecting trapezoids $\mathrm{O}(1), \mathrm{O}(2), \mathrm{O}(5), \mathrm{O}(6)$ and $\mathrm{O}(3), \mathrm{O}(4)$, $\mathrm{O}(7), \mathrm{O}(8)$ are given with the $\sigma$ values for $\mathrm{Zr} T_{4}, \mathrm{Nb} T_{4}^{+}$, $\mathrm{Sc} T_{4}^{-}$and idealized polyhedra in Table 3(a). A comparison of these values shows that the $\mathrm{ZrO}_{8}$ polyhedron is best described as a dodecahedron, distorted slightly towards a bicapped trigonal prism.

Calculations of eight-coordinate geometry for tetrakischelate complexes have been made (Blight \& Kepert, 1972; Hoard \& Silverton, 1963) which are based on the minimization of the total repulsion energy obtained by summing over all donor-atom-donor-atom repulsions. The interaction between the donor atoms of each bidentate ligand is assumed to be constant. The angular parameters of a generalized eight-coordinate stereochemistry (illustrated in Fig. 3) are varied to give the most stable geometry (or geometries) at various values of the normalized bite (b): the ratio of the ligand inter-donor-atom separation to the metal-donor-atom distance.

The calculations indicate that at low values of $b(0.5$ $\rightarrow 1 \cdot 16$ ), the most stable geometry corresponds to the $D_{2 d}$ dodecahedron; as the bite increases ( $1 \cdot 14 \rightarrow 1.23$ ), two geometries of equal stability corresponding to the $D_{2 d}$ dodecahedron and $D_{2}$ square antiprism are obtained. At large normalized bites ( $1 \cdot 17 \rightarrow 1 \cdot 24$ ), the most stable geometry corresponds to a $D_{4}$ square antiprism. Two areas of uncertainty occur where a

Table 5. Bond lengths ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ in the tropolonato ligands of $\mathrm{ZrT}_{4}$. $\left(\mathrm{CHCl}_{3}\right)_{2.25}$

| Ligand | 1 | 2 | 3 | $3^{\prime}$ | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{gathered} {[\mathrm{O}(1),} \\ \mathrm{O}(2)] \end{gathered}$ | $\begin{gathered} {[\mathrm{O}(3),} \\ \mathrm{O}(4)] \end{gathered}$ | $\begin{gathered} {[\mathrm{O}(5),} \\ \mathrm{O}(6)] \end{gathered}$ | $\begin{aligned} & {\left[\mathrm{O}\left(5^{\prime}\right),\right.} \\ & \mathrm{O}(6)] \end{aligned}$ | $\begin{gathered} {[\mathrm{O}(7),} \\ \mathrm{O}(8)] \end{gathered}$ |
| $\mathrm{O}(1)-\mathrm{C}(1)$ | 1.307 (9) | 1.27 (1) | 1.33 (2) | 1.31 (2) | 1.29 (1) |
| $\mathrm{O}(2)-\mathrm{C}(7)$ | 1.310 (9) | 1.29 (1) | 1.36 (3) | 1.25 (2) | 1.29 (1) |
| $\mathrm{C}(1)-\mathrm{C}(7)$ | 1.46 (1) | 1.47 (1) | 1.43 (3) | 1.41 (3) | 1.44 (1) |
| $\mathrm{C}(1)-\mathrm{C}(2)$ | 1.38 (1) | 1.38 (1) | 1.38 (3) | 1.38 (3) | 1.39 (1) |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | 1.37 (1) | 1.37 (1) | 1.38 (3) | $1 \cdot 39$ (3) | 1.37 (2) |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | 1.39 (1) | 1.38 (1) | 1.40 (3) | 1.35 (3) | 1.34 (3) |
| $\mathrm{C}(4)-\mathrm{C}(5)$ | 1.40 (1) | 1.35 (1) | 1.33 (3) | 1.35 (3) | 1.41 (3) |
| $\mathrm{C}(5)-\mathrm{C}(6)$ | 1.35 (1) | 1.36 (1) | 1.32 (3) | 1.39 (3) | 1.38 (2) |
| $\mathrm{C}(6)-\mathrm{C}(7)$ | 1.38 (1) | 1.42 (1) | 1.45 (3) | 1.41 (3) | 1.39 (2) |
| $\mathrm{C}(7) \mathrm{C}(1) \mathrm{C}(2)$ | 128 (1) | 124 (1) | 127 (2) | 126 (2) | 129 (1) |
| $\mathrm{C}(1) \mathrm{C}(2) \mathrm{C}(3)$ | 129 (1) | 133 (1) | 129 (2) | 131 (2) | 128 (2) |
| $\mathrm{C}(2) \mathrm{C}(3) \mathrm{C}(4)$ | 129 (1) | 126 (1) | 128 (2) | 127 (2) | 122 (2) |
| $\mathrm{C}(3) \mathrm{C}(4) \mathrm{C}(5)$ | 127 (1) | 128 (1) | 129 (3) | 128 (2) | 125 (3) |
| $\mathrm{C}(4) \mathrm{C}(5) \mathrm{C}(6)$ | 129 (1) | 130 (1) | 129 (3) | 131 (2) | 129 (2) |
| $\mathrm{C}(5) \mathrm{C}(6) \mathrm{C}(7)$ | 131 (1) | 131 (1) | 130 (2) | 126 (2) | 132 (2) |
| $\mathrm{C}(6) \mathrm{C}(7) \mathrm{C}(1)$ | 126 (1) | 125 (1) | 125 (2) | 128 (2) | 124 (1) |
| $\mathrm{O}(1) \mathrm{C}(1) \mathrm{C}(7)$ | 113 (1) | 113 (1) | 110 (2) | 114 (2) | 113 (1) |
| $\mathrm{O}(2) \mathrm{C}(7) \mathrm{C}(1)$ | 113 (1) | 113 (1) | 120 (2) | 112 (2) | 114 (1) |
| $\mathrm{O}(1) \mathrm{C}(1) \mathrm{C}(2)$ | 120 (1) | 123 (1) | 123 (2) | 119 (2) | 118 (1) |
| $\mathrm{O}(2) \mathrm{C}(7) \mathrm{C}(6)$ | 121 (1) | 122 (1) | 114 (2) | 120 (2) | 121 (1) |

choice of two possible geometries exists: $b=1 \cdot 13-$ 1.17 ( $D_{2 d}$ dodecahedron and $D_{2}$ square antiprism), and $b=1 \cdot 17 \rightarrow 1 \cdot 22\left(D_{2}\right.$ square antiprism and $D_{4}$ square antiprism). The angular parameters for the tetrakistropolonates ( $b=1.13 \rightarrow 1.16$ ) are given in Table 3 together with the parameters produced for the $D_{2 d}$ dodecahedron and $D_{2}$ square antiprism by the calculations described above. The angular parameters $\theta_{A}$ and $\theta_{B}$ serve as the most useful coordinates with which to separate different stereochemistries. At $b=$ $1 \cdot 15$, a projection onto the $\theta_{A}-\theta_{B}$ plane shows the minima corresponding to the $D_{2 d}$ dodecahedron and $D_{2}$ square antiprism lying in a shallow trough; the values of $\theta_{A}$ and $\theta_{B}$ for the tetrakistropolonates place them at different points in the bottom of the same trough between the two idealized geometries. The extent to which the tropolonates are distorted from $D_{2 d}$ dodecahedral geometry towards a $D_{2}$ square antiprism increases in the series $\mathrm{Zr}_{4}(b=1 \cdot 145), \mathrm{Nb} T_{4}^{+}(b=$ $1 \cdot 16)$ and $\mathrm{Sc} T_{4}^{-}(b=1 \cdot 13)$. [It should be noted that the $C_{2 v}$ bicapped trigonal prism use by Porai-Koshits \& Aslanov (1972) in their analysis of eight-coordinate geometry would also lie in the same trough, midway between the $D_{2 d}$ dodecahedron and the $D_{2}$ square antiprism.]

The values of $\varphi_{A}$ and $\varphi_{B}$ (the angles that metal-donor-atom bonds make with the approximate fourfold inversion axis) for the $M T_{4}$ species are consistently lower than the values predicted by the calculations, and reflect the close contacts between atoms $\mathrm{O}(1)$ and $\mathrm{O}(6)$, and $O(4)$ and $O(7)$ (Fig. 1). It has been noted previously (Davis \& Einstein, 1975) that such non-
imposed short contacts always occur between donor atoms of approximately coplanar adjacent ligands where the possibility exists for overlap of lone pairs of electrons on each donor atom, and interaction with empty $d$ orbitals on the metal. The lower values of $\varphi_{A}$ and $\varphi_{B}$ have been attributed to lengthening of $M-(A$ donor atom) bonds relative to $M-(B$ donor atom $)$ bonds as a result of the more highly repulsive bonds exerted on each $A$ donor atom. The ratio of $M-A / M-B$ for the tetrakistropolonates is 1.01 , but it is not clear why the $M-A$ bonds should increase in length to relieve repulsive forces only to then adjust to give close contacts (and subsequent high repulsive energy). This would be explained, however, by invoking the attractive force resulting from lone-pair interaction which would 'cushion' the high repulsive forces caused by close contact.

## Tropolonate ligands and chloroform molecules

Bond lengths and angles within the tropolonate ligands are given in Table 5 and include values for both positions of ligand 3. The dimensions do not differ significantly from those obtained in previous structural studies on metal tropolonates (Guggenberger \& Muetterties, 1972; Davis \& Einstein, 1974, 1975). The seven-membered rings are very nearly planar in each ligand, with slight twisting of the C skeleton relative to the plane formed by the metal and O donor atoms, the angle of twist ranging from $1.05^{\circ}$ (ligand 3) to $9.33^{\circ}$ (ligand 1).
$\mathrm{C}-\mathrm{Cl}$ bond lengths within the chloroform molecules of crystallization average $1.71 \AA$, and the $\mathrm{Cl}-\mathrm{C}-\mathrm{Cl}$ angles average $111^{\circ}$.

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# Structure Cristalline du Bis(malonato)béryllate de Potassium Hémihydraté: $\mathrm{K}_{2}\left[\mathrm{Be}\left(\mathrm{CO}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2}\right)_{2}\right] \cdot \frac{1}{2} \mathrm{H}_{2} \mathrm{O}$ 

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Crystals of potassium bis(malonato)beryllate hemihydrate, $\mathrm{K}_{2}\left[\mathrm{Be}\left(\mathrm{CO}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2}\right)_{2}\right] \cdot \frac{1}{2} \mathrm{H}_{2} \mathrm{O}$, are monoclinic, space group $C 2 / c$, with $a=22.082$ (3), $b=9.486$ (2), $c=15.183$ (4) $\AA, \beta=140.41$ (3) ${ }^{\circ}$ and $Z=8$. Mo $K \bar{\alpha}$ intensities were collected on an automatic four-circle diffractometer and the structure was determined by means of the Patterson function and Fourier syntheses. An anisotropic full-matrix least-squares refinement was performed yielding a final $R$ of 0.035 for the 1958 actually measured reflexions. The Be atom and two malonato groups make up the complex $\left[\mathrm{Be}\left(\mathrm{CO}_{2} \mathrm{CH}_{2} \mathrm{CO}_{2}\right)_{2}\right]^{2-}$ anion in which each ligand contributes, by means of two chelating O atoms, to a tetrahedral coordination of the Be atom with $\mathrm{Be}-\mathrm{O}$ bond lengths between 1.609 (3) and 1.623 (3) A. Dihedral angles between the COO and CCC planes in some malonic acid compounds are compared.


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